# Pairwise Alignment 

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## Review: Tips and tricks

Making a file executable:
chmod "a+x" pydotter.py
Handling file/directory names with spaces:
cd My $\backslash$ Directory $\backslash$ with $\backslash$ Spaces
or
cd "My」Directory」with Spaces"

## Review: Tips and tricks

Killing a process on OS $X$ :

- Try ctrl-c
- If that doesn't work:
- ps -awx | grep name_of_process
- First column in ps output is PID (process ID)
- kill PID
- If that doesn't work:

```
kill -KILL PID
```

- On Linux:
ps -ealf | grep name_of_process


## Review: Content

- FASTA files
>Name Free-form annotation
MGCLLIMKEGGPGRKKHKLIVMLYLDENQ
EHELPIMTRAPPEDINADNAMACHINEW NQEDLYMNILKKHGPPGEDEDRKHEDEDG


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- Dotplots: unbiased plot of all possible ungapped alignments of two sequences.


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- Residues with equivalent functional roles are paired
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- The sequence alignment maximizes a similarity function


## Deriving scores from alignments

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Log odds (LOD) score:

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- If evolution is uniform over time, then PAM matrices for larger evolutionary steps can be generated by multiplying PAM1 by itself (so, higher numbered PAM matrices represent greater evolutionary distances).
- The BLOSUM matrices were determined from automatically generated ungapped alignments. Higher numbered BLOSUM matrices correspond to smaller evolutionary distances. BLOSUM62 is the default matrix for BLAST.


## BLOSUM80



## BLOSUM62



## BLOSUM45



In log space, multiplication and division become addition and subtraction:

$$
\begin{aligned}
\log (x y) & =\log (x)+\log (y) \\
\log (x / y) & =\log (x)-\log (y)
\end{aligned}
$$

Therefore, exponentiation becomes multiplication:

$$
\log \left(x^{y}\right)=y \log (x)
$$

Also, we can change of the base of a logarithm like so:

$$
\log _{A}(x)=\log (x) / \log (A)
$$

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We find an optimal alignment by finding $x$ and $y$ that maximize $S$.



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## 0000000000000

Binomial formula:

$$
\begin{gathered}
\binom{k}{r}=\frac{k!}{(k-r)!r!} \\
\binom{2 n}{n}=\frac{(2 n)!}{n!n!}
\end{gathered}
$$

Stirling's approximation:

$$
\begin{gathered}
x!\approx \sqrt{2 \pi}\left(x^{x+\frac{1}{2}}\right) e^{-x} \\
\binom{2 n}{n} \approx \frac{2^{2 n}}{\sqrt{\pi n}}
\end{gathered}
$$

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The best alignment of any pair of subsequences is independent of the global alignment.

## Dynamic Programming




Needleman-Wunsch Global Alignment


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## Needleman-Wunsch Global Alignment



## Alignment speeds

- DOTTER: $O\left(n^{2}\right)$
- Exhaustive search: $\frac{2^{2 n}}{\sqrt{\pi n}}$
- Dynamic programming: $O\left(n^{2}\right)$ to $O\left(n^{3}\right)$


## Setting gap penalties in CLUSTALX



## Annotating features in JALVIEW


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 $25-$－KKRFIDRNSRVATG－LSGEEEOPLL－EGA－NP 64
21 LVRKKSL－BONLIKNGKL．．．KD－FLKTHKHMP 48 65 －R．－SEEE．．．GD IVALKNYMNADYFGEIGVGT 92
$49 A S K Y F E A A A L I G D-E F L E N Y L D T E Y F G T I G I G T 81$ 93 PPOKFTVIFDTGSSNLWVP SARCYFGIACYLFSR 126 127 YKAGASS TYKKNGKPAAIOTGTGSIAGYFSEDSV150 127 YKAGASSTYKKNGKPAAIOYGTGSIAGYFSEDSV160
115 ENEDDSSTFEATSQELSITYGTGSMTGILGTDTVI48 161 TVGDLVVKODEF－TEATKEPGITFLV．AKFDGIL192
149 DUGGISDTNGIFGLSETT－EPG．SFLYYAFFDGILIB0 149 QNGGISDTNG1FGLSET－EPG－SFLYYAFFDGILIBO 193 GLGFKE SV－OKAVPVWYKMIEQGLVS－DFVFSF 224
161 GLAMRSISASO－ATPVFONLWDRLVSOD－LFSY 212 225 WLNRHUDEGEGGEI IFGGMDPKHYVGEHTYVPUT 258
213 YLSSN－D日S－GSVMLLGGIDSSYYTGSLNMPVS 24 273 YLSSN－DDS－GSVULLGGIDSSYYTGSLNWYPVS 244 259 QKG MOFDMGD－VLVGGKSTGFGAGGCAA IADSO 291
245 VEGYMOITL－DSITMDGETIA－CSGGCCAIVDTG 276
 326 YEOQILDLLLAETOPKKICSOVOLCTFDETRGVS 359
293

 428 GSLGSMPDIEFTIGGKKFALKPEEYILKVGEGAA 461 31s－SL．－－FDIVFIINGVQYPLSFSAMILQ－DDDS． 340 462 AOC। BEF TAMDIPRPRGPLWILGDVFMGPYHTVF 495 $341-$－$T$ TGGFEGMDVPTSSGELWILGDVFIRQYYTVF 372

Sequence 2ID：all $164504 \mid$ ob｜AAA31096．1］Residue：ASN（47）

## Annotating features in JALVIEW



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1 MGTRGLALALLAAVLLLOTVLPAASEAEGLVRIA 34
1 M--
25 L-KKRPIDENSRVATG-LSGEEEQPLL-EGA-MPE4 ${ }_{21}$ LVR $_{B}$ Selection Edit

93 PPOKFTVIFDTG Group 26
27 YKAGASSTYKKNGKPAATO YGTGSIAGYFSEDSV160 IIS ENPDDSSTFEATSQELSITYOTGSMTGILGTDTV148 161 TVGDLUVKODEF-TEATKEPGITFLV. AKFDGIL 192
149 QUGGISDTNGIFGLSET-EPG-SFLYYAFFDGILIBO 193 GLGFKE SV-GKAVPVWYKMIEQGLVS-DFVF $\$ 224$
181 OLAYPSISASO-ATPVFDNLWDQOLVSQE-LFSY 212 225 WLNRHUDEGEGGEI IFGGMDPKHYVGEHTYVPVT 258 213 YLSSN-DDS-GSVULLGGIDSSYYTGSLNWYPVS 244 259 QKG MOFDMGD-VLVGGKSTGFCAGGCAA IADSG 291



 428 GSLGSMPDIEFTIGGKKFALKPEEYILKVGEGAA 461 428 GSLGSMPDIEFTIGGKKFALKPEEYILKVGEGAA 461
SIS-SL.--FDIVETINGVQYPLSESAMILQ-DDDS. 340 462 AOC I SCF TAMDIPFPRGPLWILGDVFMEPYHTVF 495 462 AOCI SGF TAMD IPFPRGPLWILGDVFMGPYHTVF 495
$341--C T S G F E G M D V R T S S G E L W I L G D V F I R Q Y Y T V F ~$
372

Sequence 2 ID: gil 164604 gb|AAA31096 II
equence I ID: all 1B904|emb|CAA39602.1 Residue: LY5 (35)

## Annotating features in JALVIEW



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| gi｜29904｜0mbl｜CA439602．21／2－50s Sil154604｜gb｜44．437096．21／2．385 |  |  |
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|  si｜25：60才｜gbluws1096．2｜／2－395 | 211 MMECLVSDPVFGFWLNRHVEBEGOEMFBCMDF245 199 LWDOCLVSODLFSVYLSSNDOS－GSVVLECIDSZ31 |  |
| cil79904｜emb C4439602．117－508 <br>  | $246 \mathrm{KHYVGEHTYYPVTOKGYWOFDMGDVLVGGKSTGFCz80}$ 232 STMTGLLNMXPVSVEGYWDITLDSITMDG－EI／ACz6 |  |
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| cil18904｜emb 1 Ca439602．1／2－508 <br>  |  |  |
|  si｜251604｜gk｜4433096．1／2－395 |  |  |
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## Annotating features in JALVIEW




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## Annotating features in JALVIEW



## Comparing files on *NIX

\# List all differences between two text files \# (empty output for identity)
diff HvSs.gap0.0.both.aln HvSs.gap0.0.mult.aln \# Report only whether the files differ \# (empty output for identity)
diff -q HvSs.gap0.0.both.aln HvSs.gap0.0.mult.aln
(*NIX $=$ *BSD, OS X, Solaris, Linux, Windows with Cygwin, ...)

## Homework

- Use a text or sequence editor to create a spliced variant of HvPhytepsin that can be aligned to the full HsSaposinC sequence
- Find the GenBank entries for HvPhytepsin and SsPepsinogen (tip: use the identifiers from the FASTA files) and find the corresponding transcript sequences.
- How easy is it to align the proteins vs. the transcripts?
- Can you tell if you are getting equivalent results from the two alignments?
- Try repeating this exercise for a pair of sequences where genomic sequence is available; e.g., $A$. nidulans VosA (ABQ18268.1), and H. capsulatum Ryp2 (ACB59236.1).

